# OXIDATION SCHEME OF SYMMETRICALLY DISULPHONATED NAPHTHIDINES WITH CERIUM(IV) SULPHATE* 

Karel Komers<br>Department of Physical Chemistry,<br>Institute of Chemical Technology, 53210 Pardubice

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The author derived theoretical dependences of preasymptotic slopes of the currentless $E-t$ curves (potential of an indicator redox electrode against time) on the number of equivalents, $n$, of added oxidation agent, assuming a reaction scheme of two consecutive concurrent second-order reactions involving the formation of intermediate products (a side reaction of the starting compound with the final oxidation product leading to an adduct, which undergoes consecutive bimolecular oxidations leading again to the final product). These dependences enable to determine the type of the relatively stable intermediate products and the ratios of the rate constants. The theory was applied to the oxidation of four symmetrically disulphonated naphthidines with cerium(IV) sulphate in aqueous sulphuric acid and the results were substantiated spectrophotometrically.

The oxidation of 1 -aminonaphthalene- $X$-sulphonic acids with cerium sulphate in aqueous sulphuric acid was already studied by us ${ }^{1,2}$ for $X=8$ and later ${ }^{3}$ for $X=$ 2,6 , and 7 . The intermediate products of this reaction are naphthidine derivatives, which are symmetrically disubstituted with sulpho groups in positions $7,7^{\prime}$ (compound $I$ ), $6,6^{\prime}$ (compound II), 5,5 (compound III), and $3,3^{\prime}$ (compound IV); their further oxidation plays a substantial role in the overall reaction mechanism. Therefore, we studied specially the oxidation of compounds $I-I V$ under the same conditions. The investigation of these relatively complicated and rapid reactions is rendered difficult in view of a limited choice of suitable analytical methods; we used the method of currentless $E-t$ curves and compared the results with spectrophotometric measurements of the red reaction mixtures in the course of the oxidation.

## THEORETICAL

We shall consider the following reaction scheme involving two consecutive concurrent reactions and a parallel formation of intermediate products:

[^0]

Here the subscripts of the reaction components denote their formal oxidation state, $k_{1}$ through $k_{6}$ are rate constants of the individual reaction steps. This complicated reaction scheme can be studied by analysing the dependence of the preasymptotic slope, $S$, of the $E$ - $t$ curves on the molar ratio of the starting compounds, $n=z / b$ (i.e., the ratio of the starting concentrations of compounds $Z_{1}$ and $A$ ) in a similar way as in references ${ }^{4,5}$.

The reacting mixture contains the following independent redox systems with the standard redox potentials $E_{0 i}$ :

$$
\begin{gathered}
\mathrm{A}=\mathrm{A}_{1}+\mathrm{e}\left(E_{01}\right), \quad \mathrm{AA}_{2}=\mathrm{A}_{1} \mathrm{~A}_{2}+\mathrm{e}\left(E_{03}\right), \quad \mathrm{Z}=\mathrm{Z}_{1}+\mathrm{e}\left(E_{02}\right), \\
\mathrm{A}_{1}=\mathrm{A}_{2}+\mathrm{e}\left(E_{02}\right), \quad \mathrm{A}_{1} \mathbf{A}_{2}=\mathrm{A}_{2} \mathrm{~A}_{2}+\mathrm{e}\left(E_{04}\right) .
\end{gathered}
$$

The general equation of the $E-t$ curve ${ }^{6}$ takes by neglecting the electrode reaction the form

$$
\begin{equation*}
\frac{\sum \mathscr{R}_{i} P_{\alpha_{1}}\left(\mathrm{~A}_{i}\right)+\mathscr{R}_{z} P_{\alpha z}\left(\mathrm{Z}_{1}\right)}{\sum \mathscr{R}_{i} P_{1-x_{i}}\left(\mathrm{~A}_{\mathrm{i}}\right)+\mathscr{R}_{\mathrm{z}} P_{1-\alpha z}(\mathrm{Z})}=1, \tag{I}
\end{equation*}
$$

where the dimensionless relative concentrations of the reactants are expressed as $\left(\mathrm{A}_{\mathrm{i}}\right)=\left[\mathrm{A}_{\mathrm{j}}\right] / b$, $\left(Z_{i}\right)=\left[Z_{1}\right] / b$ (the brackets refer to the actual concentrations of the reactants).

Further we shall make the following simplifying assumptions: 1 ) The reaction components $\mathrm{A}_{1}$ and $\mathrm{A}_{2} \mathrm{~A}_{2}$ are during the reaction in a stationary state and their concentration is considered negligible. The compound $A_{1}$ is an unstable one-electron oxidation product (a frce radical), the adduct $\mathrm{A}_{2} \mathrm{~A}_{2}$ decomposes rapidly to $2 \mathrm{~A}_{2}$.
2) The standard redox potential of the reaction $Z=Z_{1}+e$ (of the oxidant), $E_{0 Z}$, is much higher than that of the other redox systems present in the mixturc. Therefore, only the term $\mathscr{R}_{z} P_{a z}\left(Z_{1}\right)$ in Eq. (I) plays a role (owing to a high value of $P_{\alpha z}$ ), whereas the terms $\mathscr{R}_{1} P_{1-\alpha_{1}}\left(\mathrm{~A}_{1}\right)$ and $\mathscr{R}_{Z} P_{1-\alpha Z}(Z)$ in the denominator can be neglected because of negligible valucs of ( $\mathrm{A}_{1}$ ) and $P_{1-\alpha z}$.
3) Of the remaining three terms in the denominator, Eq. (1), only one need be considered, whereby this equation simplifies to

$$
\begin{equation*}
\frac{\mathscr{R}_{\mathrm{z}} P_{\alpha \mathrm{z}}\left(\mathrm{Z}_{1}\right)}{\mathscr{R}_{\mathrm{i}} P_{1-\alpha_{1}}\left(\mathrm{~A}_{\mathrm{i}}\right)}=\frac{\mathscr{R}_{\mathrm{Z}} \exp \left[-\left(E-E_{0 \mathrm{Z}}\right) \alpha_{\mathrm{Z}} F / R T\right]\left(\mathrm{Z}_{1}\right)}{\mathscr{R}_{\mathrm{i}} \exp \left[\left(E-E_{0 \mathrm{i}}\right)\left(1-\alpha_{\mathrm{i}}\right) F / R T\right]\left(\mathrm{A}_{\mathrm{i}}\right)}=1 . \tag{2}
\end{equation*}
$$

Here $\left(A_{1}\right)$ stands for $(A),\left(A A_{2}\right)$ or $\left(A_{1} A_{2}\right)$, and $E$ denotes potential of the indicator electrode in the mixture of the reacting redox systems. The dependence of $E$ on the dimensionless time $\tau=b k_{1} t$ can be expressed as

$$
\begin{equation*}
(\mathrm{d} E / \mathrm{d} \tau) y_{\mathrm{iz}}=\mathrm{d} \ln \left(\mathrm{Z}_{1}\right) / \mathrm{d} \tau-\mathrm{d} \ln \left(\mathrm{~A}_{\mathrm{i}}\right) / \mathrm{d} \tau . \tag{3}
\end{equation*}
$$

The quantity $y_{i \alpha}=\left(1-\alpha_{\mathrm{i}}+\alpha_{\mathrm{z}}\right) \boldsymbol{F} / \boldsymbol{R} T$ involves the transfer coefficients $\alpha_{\mathrm{i}}$ and $\alpha_{\mathrm{z}}$ for the corresponding redox systems. The terms $\mathrm{d} \ln \left(\mathrm{Z}_{1}\right) / \mathrm{d} \tau$ and $\mathrm{d} \ln \left(\mathrm{A}_{\mathrm{i}}\right) / \mathrm{d} \tau$ can be easily obtained from differential kinctic equations for $Z_{1}$ and $A_{i}$ valid for the above-mentioned reaction scheme and expressed in dimensionless concentrations and parameters $\xi=k_{3} / k_{1}, \omega=k_{4} / k_{1}, \sigma=$ $=k_{5} / k_{1}$ :

$$
\begin{align*}
& -\mathrm{d}(\mathrm{~A}) / \mathrm{d} \tau=(\mathrm{A})\left(\mathrm{Z}_{1}\right)+\xi(\mathrm{A})\left(\mathrm{A}_{2}\right),  \tag{4}\\
& \mathrm{d}\left(\mathrm{AA}_{2}\right) / \mathrm{d} \tau=\xi(\mathrm{A})\left(\mathrm{A}_{2}\right)-\omega\left(\mathrm{AA}_{2}\right)\left(\mathrm{Z}_{1}\right),  \tag{5}\\
& \mathrm{d}\left(\mathrm{~A}_{1} \mathrm{~A}_{2}\right) / \mathrm{d} \tau=\omega\left(\Lambda \mathrm{A}_{2}\right)\left(\mathrm{Z}_{1}\right)-\sigma\left(\mathrm{A}_{1} \mathrm{~A}_{2}\right)\left(\mathrm{Z}_{1}\right),  \tag{6}\\
& \mathrm{d}\left(\mathrm{Z}_{1}\right) / \mathrm{d} \tau=2(\mathrm{~A})\left(\mathrm{Z}_{1}\right)+\omega\left(\mathrm{AA}_{2}\right)\left(\mathrm{Z}_{1}\right)+\sigma\left(\mathrm{A}_{1} \mathrm{~A}_{2}\right)\left(\mathrm{Z}_{1}\right),  \tag{7}\\
& \mathrm{d}\left(\mathrm{~A}_{2}\right) / \mathrm{d} \tau=(\mathrm{A})\left(\mathrm{Z}_{1}\right)-\xi(\mathrm{A})\left(\mathrm{A}_{2}\right)+2 \sigma\left(\mathrm{~A}_{1} \mathrm{~A}_{2}\right)\left(\mathrm{Z}_{1}\right) \tag{8}
\end{align*}
$$

The rclative concentrations of the reactants fulfil the conditions

$$
\begin{gather*}
(\mathrm{A})+\left(\mathrm{A}_{2}\right)+2\left(\mathrm{AA}_{2}\right)+2\left(\mathrm{~A}_{1} \mathrm{~A}_{2}\right)=1,  \tag{9a}\\
\left(\mathrm{Z}_{1}\right)+(\mathrm{Z})=n, \tag{9b}
\end{gather*}
$$

and the condition for the number of transferred electrons is

$$
\begin{equation*}
2\left(\mathrm{~A}_{2}\right)+2\left(\mathrm{AA}_{2}\right)+3\left(\mathrm{~A}_{1} \mathrm{~A}_{2}\right)=(\mathrm{Z}) \tag{9c}
\end{equation*}
$$

Our aim is to find the dependence $S=(\mathrm{d} E / \mathrm{d} \tau) y_{\mathrm{iz}}-n$ for the preasymptotic portion of the $E-t$ curves, where the reaction is practically finished. Since the proportionality coefficient $y_{\mathrm{iz}}$ is unknown, the quantity $S$ is determined as $(\mathrm{d} E / \mathrm{d} \tau)_{\mathrm{n}} /(\mathrm{d} E / \mathrm{d} \tau)_{\mathrm{n}=0}$, i.e., it is normed by the coordinate of the starting point $S=2, n=0$.

In the final reaction stage we have (in addition to the compound $Z$ ) in the interval $n(0 ; 1)$ to deal only with compounds A and $\mathrm{AA}_{2}$ in concentrations $(\mathrm{A})_{\infty}=1-n$ and $\left(\mathrm{AA}_{2}\right)_{\infty}=n / 2$. For $n(1 ; 1 \cdot 5)$ we have $(\mathrm{A})_{\infty}=0\left(\mathrm{AA}_{2}\right)_{\infty}=(3-2 n) / 2$ and $\left(\mathrm{A}_{1} \mathrm{~A}_{2}\right)_{\infty}=n-1$; for $n(1 \cdot 5 ; 2)$ we have $(\mathrm{A})_{\infty} \equiv\left(\mathrm{AA}_{2}\right)_{\infty}=0\left(\mathrm{~A}_{1} \mathrm{~A}_{2}\right)_{\infty}=2-n$, $\left(\mathrm{A}_{2}\right)_{\infty}=2 n-3$; and for $n>2$ we have $\left(\mathrm{A}_{2}\right)_{\infty}=1,\left(\mathrm{Z}_{1}\right)_{\infty}=n-2$. By substituting the terms $d \ln \left(Z_{1}\right) / d \tau$ and $d \ln \left(A_{i}\right) / d \tau$, calculated from Eqs (4)-(8), into Eq. (3), considering the given conditions for different intervals of $n$ values and rearranging we obtain the theoretical $S-n$ dependences for the preasymptotic portions of the $E-t$ curves, which are given in Table I. These are shown graphically in Fig. 1. In the case where the term with (A) in the denominator of Eq. (2) becomes important, the dependence in the interval $n(0 ; 3)$ consists of four linear portions, whereas in the cases where $\left(\mathrm{AA}_{2}\right)$ or $\left(\mathrm{A}_{1} \mathrm{~A}_{2}\right)$ become important, it consists of three linear portions. The points where the linear dependence is broken characterize not only the type of intermediate reaction products (the break at $n=1$ corresponds to the formation of a one--electron product $\mathrm{AA}_{2}$, that at $n=1.5$ to $\mathrm{A}_{1} \mathrm{~A}_{2}$ with a one and a half-electron oxidation stage, that at $n=2$ to a two-electron oxidation to $A_{2}$ ), but also the ratios of the corresponding rate constants $\omega, \sigma$, and $\xi$.

Table I
Reaction Scheme: Equations for $S-n$ Dependences in Different Intervals of $n$ Values

| Interval <br> $n$ | Important term <br> in denominator <br> of Eq. (2) | Function $S(n)$ |
| :---: | :---: | :--- |

$0 ; 1 \quad \mathrm{~A}$ or $\mathrm{A}_{1} \mathrm{~A}_{2}$ or $\mathrm{AA}_{2} \quad S=n(2-\omega / 2)-2$
1; 1.5
$1 \cdot 5 ; 2{ }^{2}$

2
A or $\mathrm{A}_{1} \mathrm{~A}_{2}$ or $\mathrm{AA}_{2} \quad S=n(\omega-\sigma)+\sigma+1.5 \omega$
A
$S=n(\sigma-2 \xi)-(2 \sigma+3 \xi)$
$\mathrm{AA}_{2}$ or $\mathrm{A}_{1} \mathrm{~A}_{2}$
$S=\sigma(n-2)$
A $\quad S=n-2+\xi$
$\mathrm{AA}_{2} \quad S=\omega(n-2)$
$\mathrm{A}_{1} \mathrm{~A}_{2} \quad S=\sigma(n-2)$


Fig. 1
Illustrative Dependences of $S$ on $n$ for Reaction Scheme

Beginning from $n=1 \cdot 5$, the solid line refers to the case where the term (A) in the denominator of (2) plays a role, the dashed line refers to the case where the terms with $\left(A A_{2}\right)$ or ( $A_{1} A_{2}$ ) become important. The conditions $\omega<4, \sigma>\omega$ apply.


Fig. 2
Dependence of $\mathrm{d} E / \mathrm{d} t$ on $n$ for Compounds $I$ (1), $I I$ (2), and $I V$ (4)

Numbers of the curves refer to the compounds. Compounds $I$ and $I I$ were oxidised at $\mathrm{H}_{0}=-3$, compound $I V$ at $\mathrm{H}_{0}=-4$; $20^{\circ} \mathrm{C}$.

## EXPERIMENTAL

## Apparatus

The $E-t$ curves were recorded by using the experimental equipment described earlier ${ }^{7}$ without an inert atmosphere in view of the relative stability of the strongly acidic solutions of compounds $I-I V$. The indicator electrode was smooth platinum; a saturated $\mathrm{Hg} / \mathrm{Hg}_{2} \mathrm{SO}_{4}$ electrode served as reference.

The dependences of the absorbance of the reaction mixture, $a$, at a suitable wave length on the time, $t$, with n as parameter were measured on a spectrograph of the type Specord UV-VIS (Zeiss, Jena, GDR) with a built-in mixing and tempering adapter ${ }^{8}$ enabling a perfect mixing of the reaction components within a second and tempering in the interval from --20 to $+60^{\circ} \mathrm{C}$ with an accuracy to $\pm 0 \cdot 1^{\circ} \mathrm{C}$ in 2 cm thick glass cuvettes holding 30 ml of solution. With compound $I V$, which was extremely rapidly oxidised, a stop-flow apparatus of the type D 110 (Durrum Instrument Corp., USA) was used, in which the time of mixing was about $10^{-3} \mathrm{~s}$ at a cuvette thickness of 2 cm . The measurement was carried out at the maximum absorbance of the red oxidation mixture, i.e., at 525 nm with compounds $I$ and $I I$, at 510 nm with compound $I I I$, and at 570 nm with $I V$. The dependence of the maximum absorbance, $a_{\infty}$, at the final stage of the reaction on $n$ was obtained from a set of $a-t$ curves by plotting the values of $a$ for sufficiently large values of $t$, where the absorbance was constant, against $n$.

## Chemicals

The compounds $I-I V$ were prepared by the method described by $\mathrm{us}^{2}$ except that the diazonium salt was reduced to the azo compound by a saturated aqueous solution of $\mathrm{Na}_{2} \mathrm{SO}_{3}$ in the medium of sodium acetate ( 16 g of the acetate in $75 \mathrm{~cm}^{3}$ of water). Thus, the yields were somewhat higher. A standard solution of the starting compound was prepared by weighing, suspending in redistilled water, adding pyridine dropwise (reagent grade) to dissolution and making up to the mark with water. The maximum concentration of the standard solution was $0.01 \mathrm{~mol} / \mathrm{dm}^{3}$. Since it was sensitive against oxidation (it turned brown), it was stored in the dark and solutions older than one week were discarded. The factor of the standard solution was determined by potentiometric titration with a standard solution of KOH with an antimony-saturated calomel electrode couple. The starting reaction mixture containing $10^{-4}-10^{-5} \mathrm{~mol} / \mathrm{dm}^{3}$ reactants was prepared by diluting the stock solution of the pyridinium salt with the given reaction medium. A standard solution of $0.01 \mathrm{~mol} / \mathrm{dm}^{3} \mathrm{Cc}\left(\mathrm{SO}_{4}\right)_{2}$ was prepared from $\mathrm{Ce}\left(\mathrm{SO}_{4}\right)_{2} .4 \mathrm{H}_{2} \mathrm{O}$ of reagent grade (Merck, GFR) by dissolving in a diluted sulphuric acid whose pH was the same as that of the reaction medium. The factor of this solution was determined potentiometrically with a standard solution of $\mathrm{Fe}\left(\mathrm{NH}_{4}\right)_{2}\left(\mathrm{SO}_{4}\right)_{2}$. The reaction medium was aqueous sulphuric acid whose acidity was defined by the Hammett acidity function $\mathrm{H}_{0}$.

## RESULTS AND DISCUSSION

The oxidation of compounds $I-I V$ was studied at room temperature mainly in strongly acidic media ( $\mathrm{H}_{0}$ from -3 to -4 ), where the red products were relatively most stable (about 10 min at $20^{\circ} \mathrm{C}$ ). At a lower acidity, these products decompose more rapidly to practically colourless compounds and the reaction rate increases considerably.

Compounds I and II
E-t Curves
By plotting the potential of the indicator electrode, $E_{\infty}$, at the final stage of the reaction (read from the set of $E-t$ curves with $n$ as parameter) against $n$, we obtain a curve with a potential jump for $n=2$, an evidence for a two-electron oxidation. Since a trimolecular reaction $\left(A+2 Z_{1} \rightarrow \ldots\right)$ is improbable, a consecutive oxidation $A \rightarrow A_{1} \rightarrow A_{2}$ must form the base of the oxidation schome. The form of the $\mathrm{d} E / \mathrm{d} t-n$ curves (Fig. 2, curves 1 and 2) with breaks for $n=1,1.5$ and 2 suggests that the consecutive oxidation is accompanied by the formation of intermediate products, e.g., according to the reaction scheme given in the theoretical part by the compounds $\mathrm{AA}_{2}, \mathrm{~A}_{1} \mathrm{~A}_{2}$. Then, of course, the ordinates of the mentioned breaks, eventually of the point for $n=3$ must correspond to the ratios of the rate constants $\omega, \sigma$, and $\xi$ on the $S-n$ curve (Fig. 1). In this way we found the values of these ratios for the oxidation of compounds $I$ and $I I$ and these are given in Table II.

## Spectrophotometry

The ratio of actual absorbances measured in a reaction mixture in such a region of the visible spectrum where neither the starting compounds $A$ and $Z_{1}$ nor the product $Z$ absorb fulfils the equatior

$$
\begin{equation*}
a\left(\lambda_{1}, t\right) / a\left(\lambda_{2}, t\right)=\text { const } \tag{10}
\end{equation*}
$$

This requires the validity of the relation $\varepsilon_{i}(\lambda)=k_{i} \varepsilon_{A_{2}}(\lambda)$ with $k_{1}$ independent of $\lambda$, where $\varepsilon_{i}$ denotes molar decadic absorption coefficients of all oxidation products of the compound A in the reaction mixture.

Table II!
Ratios of Rate Constants $\omega, \sigma$, and $\xi$ for Oxidation of Compounds $I$ and $I I$ at $20^{\circ} \mathrm{C}$ with $\mathrm{Ce}\left(\mathrm{SO}_{4}\right)_{2}$ in Aqueous $\mathrm{H}_{2} \mathrm{SO}_{4}$ Obtained by Analysis of $S-n$ Curves

Acidity of the medium is given by the Hammett acidity function $\mathrm{H}_{0}$.

| Compound | $\mathrm{H}_{0}$ | $\omega$ | $\sigma$ | $\xi$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | -3 | 96 | 74 | 8 |
| II | -4 | 15 | 18 | 6 |
|  | -3 | 23.2 | $27 \cdot 4$ | 15 |
|  | -2 | 15 | 16 | $18 \cdot 6$ |
|  | -1 | 14 | $12 \cdot 8$ | 5 |

Dependence of $a_{\infty}$ on $n$
This dependence increases linearly with $n$ up to $n=2$ attaining a constant value for $n>2$. The break at $n=2$ is an evidence for a two-electron oxidation. We assume that the reaction mixture contains the species $A, A_{2}, A_{2}, A_{1} \mathrm{~A}_{2}, \mathrm{Z}_{1}$, and Z , of which $A, Z_{1}$ and $Z$ do not absorb light in the given region of wave lengths. Based on the final concentrations $\left(\mathrm{A}_{\mathrm{i}} \mathrm{A}_{2}\right)_{\infty}$, the total absorbancy of the final reaction mixture is given by the equations

$$
\begin{array}{ll}
n(0 ; 1): & a_{\infty}=\frac{1}{2} \varkappa_{02} n \\
n(1 ; 1 \cdot 5): & a_{\infty}=\varkappa_{02}(3-2 n) / 2+\varkappa_{12}(n-1) \\
n(1 \cdot 5 ; 2): & a_{\infty}=\varkappa_{12}(2-n)+\varkappa_{2}(2 n-3) \\
n>2: & a_{\infty}=\varkappa_{2},
\end{array}
$$

where $\varkappa_{\mathrm{i} 2}=\varepsilon_{\mathrm{i} 2} d b$ and $d$ is the thickness of the cuvette. The mentioned experimental dependence can be expressed as $a_{\infty}=$ const. $n$ for $n \leqq 2$ and $a_{\infty}=2$. const for $n>2$; this can be brought into agreement with the theory only if $\varepsilon_{02} \equiv \varepsilon_{2}$ and $\varepsilon_{12}=$ $=\frac{3}{2} \varepsilon_{2}$. This in turn implies that only the species $A_{2}$ is responsible for the absorption of light in $\mathrm{AA}_{2}$, whereas the absorbancy of $\mathrm{A}_{1} \mathrm{~A}_{2}$ is due also to the species $\mathrm{A}_{1}$, which has a radical character. It can be shown by substitution into $(11 b, c)$ that the lincarity of the $a_{\infty}-n$ dependence is preserved also in the interval $n(1 ; 2)$ with a maximum relative error of $\pm 13 \%$ for $n=1 \cdot 5$, if the value of $\varepsilon_{12}$ lies in the interval from $1 \cdot 4 \varepsilon_{2}$ to $1 \cdot 7 \varepsilon_{2}$.

## Dependence of $a$ on $t$

We assume on the basis of the values of $\omega, \sigma$, and $\xi$ following from the $S-n$ curves (Table II) that the intermediate products $\mathrm{AA}_{2}$ and $\mathrm{A}_{1} \mathrm{~A}_{2}$ are during the reaction up to a certain conversion in a stationary state. This was substantiated by calculating the theoretical trajectories $\left(\mathrm{A}_{\mathrm{i}}\right)-\left(\mathrm{Z}_{1}\right)$ from Eqs (4) - (8) by an analogue computer (Fig. 3). The values of $\omega, \sigma$ and $\xi$ were chosen close to those in Table II, valid for $20^{\circ} \mathrm{C}$ and $\mathrm{H}_{0}=-3$. A stationary state of the components $\mathrm{AA}_{2}$ and $\mathrm{A}_{1} \mathrm{~A}_{2}$ exists in the reacrion mixture for compound $I(\xi=10, \omega=100, \sigma=75)$ and $n=1.5$ or 2 practically in the whole range of the reaction times. During oxidation of compound II ( $\zeta=15, \omega=20, \sigma=30$ ), this criterion holds for $n=2$ up to about $80 \%$ conversion, for $n=1.5$ and species $\mathrm{A}_{1} \mathrm{~A}_{2}$ up to about $70 \%$ and for $\mathrm{AA}_{2}$ up to about $60 \%$ conversion. In this time interval, the $a-t$ dependence represents naturally only the function $\left(\mathrm{A}_{2}\right)-t$, since $a(n) / a_{\infty}(n=2)=\left(\mathrm{A}_{2}\right)$.

## Linearization of the a-t Function

The differential kinetic equation describing the $\left(\mathrm{A}_{2}\right)-t$ function for the considered scheme (sce Theoretical) with the assumption of a stationary state for $A_{1}, A_{2}, A_{1} A_{2}$, and $A_{2} A_{2}$ has the form

$$
\begin{equation*}
\mathrm{d}\left(\mathrm{~A}_{2}\right) / \mathrm{d} \tau=b\left[k_{1}(\mathrm{~A})\left(\mathrm{Z}_{1}\right)+k_{3}(\mathrm{~A})\left(\mathrm{A}_{2}\right)\right] \tag{12}
\end{equation*}
$$

This equation can be solved with the conditions

$$
\begin{equation*}
(\mathrm{A})+\left(\mathrm{A}_{2}\right)=1, \quad(\mathrm{Z})+\left(\mathrm{Z}_{1}\right)=n, \quad(\mathrm{Z})=2\left(\mathrm{~A}_{2}\right) \tag{13}
\end{equation*}
$$

in a closed form; the result can be expressed as a special case of a general functional dependence represented by the sum of two exponentials, which can be linearized ${ }^{9}$. We arrive at the equation

$$
\begin{equation*}
\mathrm{Y}=[\exp (\gamma \Delta t)+1] \mathrm{X}-\exp (\gamma \Delta t), \tag{14}
\end{equation*}
$$

where

$$
\begin{aligned}
& \mathrm{Y}=\left[\left(\mathrm{A}_{2}\right)_{\infty}-\left(\mathrm{A}_{2}\right)\right] /\left[\left(\mathrm{A}_{2}\right)_{\infty}-\left(\mathrm{A}_{2}\right)_{2}\right]=\left[a_{\infty}-a(t)\right] /\left[a_{\infty}-a\left(t_{2}\right)\right] \\
& \mathrm{X}=\left[\left(\mathrm{A}_{2}\right)_{\infty}-\left(\mathrm{A}_{2}\right)\right] /\left[\left(\mathrm{A}_{2}\right)_{\infty}-\left(\mathrm{A}_{2}\right)_{1}\right]=\left[a_{\infty}-a(t)\right] /\left[a_{\infty}-a\left(t_{1}\right)\right]
\end{aligned}
$$

The quantities X and Y can be obtained from the $a-t$ curve for a given $n$ by determining the values of $a(t), a\left(t_{1}\right), a\left(t_{2}\right)$ for $t, t_{1}$ and $t_{2}$ forming an arithmetic series.


Fig. 3
Dependences of ( $\mathrm{A}_{1}$ ) on ( $\mathrm{Z}_{1}$ ) Calculated by Analoguc Computer from Equations (4) -(7) and (11)

Curves $a, b, c$, and $d$ represent the dependences of $(A),\left(A_{2}\right),\left(A A_{2}\right)$ and ( $\left.A_{1} A_{2}\right)$ on $\left(Z_{1}\right)$, where $\left(A_{i}\right)=\left[A_{i}\right] / b$ and $\left(Z_{1}\right)=$ $=\left[\mathrm{Z}_{1}\right] / z$. Curves 1 correspond to $\xi=10$, $\omega=100, \sigma=75, n=1 \cdot 5$; curves 2 as 1 but $n=2$. Curves 3 correspond to $\xi=15$, $\omega=20, \sigma=30, n=1 \cdot 5$; curves 4 as 3 but $n=2$.

The dependence (14) corresponds to a straight line in the coordinates X , Y passing through the point $\mathrm{X}=\mathrm{Y}=1$. This linearity for a given value of $n$ is an evidence for the validity of Eq. (12); its intersection and slope give the values of $k_{1}$ and $k_{3}$, since $\gamma=b k_{3}+b k_{1}(n-2)$ for $n \neq 2$ or $\gamma=b k_{3}$ for $n=2$. As an example, Table III gives the values of $\xi=k_{3} / k_{1}$ for oxidation of compound $I$ with cerium(IV) sulphate at $5^{\circ} \mathrm{C}$ and $\mathrm{H}_{0}=-3$, obtained from the $a-t$ curves for various $n$ values. The table gives also the extent of the reaction with respect to A or $\mathrm{Z}_{1}$, up to which the $\mathrm{X}-\mathrm{Y}$ dependence can be considered linear. These data and the agreement between the values of $\xi$ from spectrophotometry and from $E-t$ curves (Table IV) suggest the correctness of the proposed scheme.

Table III
Values of $\xi$ Obtained by Lincarization of the $a-t$ Dependence with $n$ as Parameter
Data refer to compound $J$ and cerium(IV) sulphate at $5^{\circ} \mathrm{C}$ and $\mathrm{H}_{0}=-3 ; r$ is the extent of the reaction with respect to $\mathrm{Z}_{1}(n<2)$ or $\mathrm{A}(n>2)$, up to which the $\mathrm{X}-\mathrm{Y}$ dependence is linear.

| $n$ | $\boldsymbol{\xi}$ | $r$ |
| :--- | :--- | ---: | :--- |
|  |  |  |
| 0.49 | 9.40 | $50 \%$ |
| 0.98 | 10.05 | 73 |
| 1.48 | 12.10 | 71 |
| 1.97 | 9.95 | 72 |
| 2.46 | 5.04 | 77 |
| 2.95 | 15.24 | 73 |
| 3.44 | 18.83 | 85 |

Table IV
Ratios of Rate Constants $k_{3} / k_{1}=\boldsymbol{\xi}$ Determined from $S-n$ Curves, by Rectification of the $\left[\mathrm{A}_{2}\right]-t$ Dependence and by the Analogue Computer for Oxidation of Compounds $I$ and $I I$ at $20^{\circ} \mathrm{C}$

| Compound | $\mathrm{H}_{0}$ | $n$ | $\xi=k_{3} / k_{1}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | linearization | anal. comp. | $S-n$ curve |
|  |  |  |  | 5 | 6 |

## Analogue Solution

Eq. (12) and the conditions (13) were after some modifications solved on a MEDA 42 TA type analogue computer. The fact that the absorbance of the reaction mixture does not change after exhaustion of $\mathrm{Z}_{1}$ was taken into account in the circuiting. With the aid of the computing network in combination with a generator of the function $y=\ln \tau$ nomograms of the $\left(\mathrm{A}_{2}\right)-\ln \tau$ dependence with $\xi$ as parameter were obtained for selected values of $n$. Based on the agreement of the normed experimental curves $\left(\mathrm{A}_{2}\right)-\ln t$ with one of the theoretical curves, the proposed scheme was substantiated and the value of $\xi$ was determined. The difference of $\ln \tau-\ln t=\ln \left(b k_{1}\right)$ on the $x$ axis of the nomogram and experimental dependence gives the value of $k_{1}$.

It follows from Table IV that a good agreement was attained among the values of $\xi$ determined by the method of $S-n$ curves, rectification, and by the analogue computer, especially if we take into account the complexness of the reaction scheme and high overall reaction rate, since the rate constant $k_{1}$, which is the smallest one, is equal to $10^{2}-10^{3} \mathrm{dm}^{3} / \mathrm{mols}$ for both substances under the given conditions. Its magnitude was checked by calculation from the slope of the dependence $\left(A_{2}\right)$-t for $t \rightarrow 0$, where only the stcp 1 plays a role under the condition $\left[\mathrm{A}_{1}\right]_{\mathrm{L}=0} \equiv\left[\mathrm{~A}_{2}\right]_{\mathrm{I}=0}$.

## Compound IV

## E-t Curves

The dependence of $E_{\infty}$ on $n$ shows a potential step for $n=2$; an evidence for a two--electron oxidation similarly to compounds $I$ and $I I$. The $S-n$ dependence, represented in the interval $n(0 ; 2)$ by a decreasing straight line, suggests, however, another oxidation mechanism. Its experimental course (Fig. 2, curvc 4) can be explained either I) by a system of two concurrent consecutive reactions with the condition $k_{1} \ll k_{2}$, or 2) by the same scheme supplemented with dismutation of the intermediate product:

$$
2 A_{1} \underset{k_{d^{\prime}}}{\stackrel{k_{d}}{\leftrightarrows}} A+A_{2}
$$

with the condition $k_{\mathrm{d}} \gg k_{\mathrm{d}}^{\prime}$. Since the norm of the $S$ axis is not known, these two cases cannot be distinguished $(\mathrm{S}(n=0)=2$ for case $l)$, but $S(n=0)=1$ for case 2) according to ref. $\left.{ }^{4,5}\right)$. The ratio of the rate constants, $k_{2} / k_{1}$ or $k_{\mathrm{d}} / k_{\mathrm{d}}^{\prime}$, cannot be determined either. In both cases, the system behaves naturally as a sccond-order reaction with a stoichiometry of $\mathrm{A}: Z_{1}=1: 2$, so that the experimental ensemble of $E-t$ curves could be used for calculating the value of $k_{1}$ in a similar way as in the case of a simple bimolecular reaction ${ }^{10,11}$. The result of this procedure is the value of $k_{1}=8400 \mathrm{dm}^{3} / \mathrm{mol} \mathrm{s}$ for $\mathrm{H}_{0}=-4$ and $20^{\circ} \mathrm{C}$.

## Spectrophotometric Measurements

Eq. (10) holds also now and the dependence of $a_{\infty}$ on $n$ is similar to that for compounds $I$ and $I I$. Since we consider only one intermediate product, $\mathrm{A}_{1}$, in the stationary state, the $a-t$ curve measured in the visible range of the spectrum represents the $\left(\mathrm{A}_{2}\right)-t$ dependence. If we assume oxidation according to case $l$, we obtain by solving the differential equation $\mathrm{d}\left(\mathrm{A}_{2}\right) / \mathrm{d} t=b k_{1}(\mathrm{~A})\left(\mathrm{Z}_{1}\right)$ with the conditions $(\mathrm{A})+$ $+\left(\mathrm{A}_{2}\right)=1,\left(\mathrm{Z}_{1}\right)+(\mathrm{Z})=n$, and $(\mathrm{Z})=2\left(\mathrm{~A}_{2}\right)$ the following expressions:

$$
\begin{gather*}
\ln \left[\left(n-2\left(A_{2}\right)\right) /\left(1-\left(A_{2}\right)\right)\right]=b k_{1}(n-2) t+\ln n, \quad n \neq 2  \tag{15}\\
1 /\left(1-\left(A_{2}\right)\right)=1+2 b k_{1} t, \quad n=2 \tag{16}
\end{gather*}
$$

By using the experimental $a-t$ curve for a given $n$ and plotting the left sides of Eqs (15) and (16) against $t$ we obtained exactly linear dependences from which the values of $k_{1}$ were obtained. These are in good agreement with the results of analysis of the $E-t$ curves under the same conditions: $k_{1}=9780(n=1), 9670(n=1.4), 9870$ $(n=2), 9400(n=3) \mathrm{dm}^{3} / \mathrm{mols}$. By comparing the experimental dependences of $\left(\mathrm{A}_{2}\right)$ on $\log t$ for $n=1$ and 2 with nomograms calculated for the same $n$ values and case $l$ by an analogue computer we obtain an average value of $k_{1}=1 \cdot 02.10^{4}$ $\mathrm{dm}^{3} / \mathrm{mols}$.

Neither of the mentioned methods enables to distinguish the two proposed mechanisms. In case 2 with an irreversible dismutation of $A_{1}$ we obtain equations which difler from (15) and (16) only by the coefficient 0.5 in the terms containing $t$, provided that $\mathrm{d}\left(\mathrm{A}_{1}\right) / \mathrm{d} t=0$. The analogue solution showed the possibility of the same form of the $\left(\mathrm{A}_{2}\right)-t$ dependence with the condition $k_{\mathrm{d}} \approx 10^{3} k_{1} \approx 10^{7} \mathrm{dm}^{3} / \mathrm{mol} \mathrm{s}$, or $k_{2} \approx$ $\approx 500 k_{1} \approx 5.10^{6} \mathrm{dm}^{3} / \mathrm{mol} \mathrm{s}$, or if the ratios of $k_{2} / k_{1}$ and $k_{\mathrm{d}} / k_{1}$ are simultaneously larger than 20. In view of the high valuc of $k_{d}=10^{7} \mathrm{dm}^{3} / \mathrm{mols}$ for the reaction between two relatively large organic molecules of $\mathrm{A}_{1}$, the reaction assumed in case $I$ appears more probable. The necessary high rate of oxidation of $\mathbf{A}_{1}$ to $\mathbf{A}_{2}\left(k_{2}=\right.$ $=5.10^{6} \mathrm{dm}^{3} / \mathrm{mols}$ ) refers to the reaction between an organic molecule $\mathrm{A}_{1}$ and a strong oxidising agent $\mathrm{Ce}(\mathrm{IV})$.

## Compound III

It follows from the dependences of $E_{\infty}$ and $a_{\infty}$ on $n$ that the stoichiometrical ratio of $\mathrm{A}: \mathrm{Z}_{1}$ is different from that in the case of compounds $I, I I$ and $I V$ : it is equal to $1: 3$. This is an evidence for a different oxidation mechanism of compound $I I I$, which will be discussed in a subsequent communication.

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